Optimization of triple-junction hydrogenated silicon solar cell 
nc-Si:H/a-Si:H/a-SiGe:H using step graded Si$_{1-x}$Ge$_x$ layer

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ABSTRACT
This paper shows the attempt to increase the performance of triple-junction hydrogenated silicon solar cells with structure nc-Si:H/a-Si:H/a-SiGe:H. The wxAMPS software was used to simulate and optimize the design. In an attempt to increase the performance, an a-SiC:H layer on the p-layer was replaced with an a-Si:H layer and an a-SiGe layer was replaced with a step graded Si$_{1-x}$Ge$_x$ layer. Then, to achieve the best performing device, we optimized the concentration of germanium and thickness of the step graded Si$_{1-x}$Ge$_x$ layer. The result shows that the optimum concentration of germanium in the p-i upper layer and i-n lower layer are 0.86 and 0.90, respectively and the optimum thicknesses are 10 nm and 230 nm, respectively. The optimized device performed with an efficiency of 19.08%, adding 3 more percent of efficiency from the original design. Moreover, there is a significant possibility of increasing the efficiency of a triple-junction solar cell by modifying it into a step graded Si$_{1-x}$Ge$_x$ layer.

Keywords:
Hydrogenated silicon
Si$_{1-x}$Ge$_x$
Solar cell
Step graded
Triple-junction

1. INTRODUCTION
In the development of solar cell technology, multijunction (MJ) solar cells are standardly used to increase efficiency. In contrast to a single-junction solar cell, an MJ solar cell is made by stacking several semiconductor junctions, which allow a wider range of wavelengths to be converted into electricity. Recent
progress in MJ solar cells, especially with semiconductor material III-V, has the potential to achieve conversion efficiencies of more than 40% [1-3]. However, the common use of MJ solar cells with III-V materials is still limited due to the high cost of its fabrication and the rare materials used. To overcome these limitations, different design approaches and materials are needed. One of the solutions is the integration of semiconductor material III-V on a low-cost Si substrate. The development of III-V/Si can significantly reduce the cost of solar cells without reducing its efficiency [4, 5].

MJ solar cells are not limited to III-V material. Hydrogenated amorphous silicon-germanium (a-SiGe:H) is another potential thin-film material for MJ silicon solar cells. Theoretically, by using SiGe alloy, the absorption ability of silicon cells can be expanded to the infrared response and hence can increase the current generation [6]. A thin-film triple-junction cell that combines hydrogenated amorphous silicon (a-Si:H) and an a-SiGe:H can achieve a stable cell efficiency of 13% [7]. Several groups also studied the triple-junction solar cell with structure a-Si:H/a-SiGe:H/nc-Si:H and can produce cells with an efficiency of 15.4% [8, 9]. Furthermore, modeling of MJ solar cells using a-SiGe:H and microcrystalline silicon were conducted [10]. Another effort to produce high-efficiency cells was performed by Ferhati et al. Incorporating muti-trench region shows an increase in the efficiency of a-SiGe:H MJ solar cells [11, 12]. Besides optimizing the device design, improving the quality of a-SiGe:H in the fabrication process can also result in a high-performance solar cell [13, 14].

However, the mentioned research did not apply the step graded Si1−xGeX to their structure. Silicon and germanium have a difference in their lattice constants, i.e. by 4.2% [15, 16]. This difference can cause a lattice mismatch, which causes a discontinuity in the SiGe layers embedded on a layer of silicon [17]. These discontinuities may create misfit dislocation defects and reduce the performance of solar cells [18]. To reduce these defects, the SiGe can be performed in stages based on the germanium concentration (step graded Si1−xGeX). The step graded layer that is added to the silicon solar cells can improve the efficiency of the cells [19, 20]. Furthermore, this technique can produce a layer of SiGe with better dislocation density, i.e. 10^7 cm^2, compared to without using the grading step, which amounts to 10^12 cm^2 [21]. In the recent development, the concept of reverse graded SiGe is introduced for GaAsP/SiGe tandem solar cells [22].

Here, we optimize the triple-junction solar cells of nc-Si:H/a-Si:H/a-SiGe:H which is based on our previous works [23]. The structure still using bulk a-SiGe:H which has a significant lattice constant mismatch. By replacing the a-SiGe:H layer with step graded Si1−xGeX:H and replacing the a-Si:H layer with an a-Si:H can improve the lattice constant mismatch, thus increasing its performance. Computer software wxAMPS was utilized to simulate and optimize the design [24]. To obtain the best performing device, we optimize the concentration and thickness of the step graded Si1−xGeX layer. Analysis of the bandgap and generation-recombination graph is also provided.

2. DEVICE DESIGN AND OPTIMIZATION

The original structure was optimized by searching the optimum thickness of the active layer, which resulted in a device with an efficiency of 15.73% [23]. To increase its efficiency further, we optimized the device structure in three stages, as shown in Figure 1. Additionally, flowchart of the optimization process can be found in Figure 2.

![Figure 1](image)

(a) (b) (c)

Figure 1. Three structures of the triple-junction solar cell used in this research, (a) The original structure (nc-Si:H/a-Si:H/a-SiGe:H), (b) The first and second stages of the optimization structure, (c) The third stage of the optimization structure using step grading.
First, the active layer compound of a-SiGe:H is replaced with the Si$_{1-x}$Ge$_x$ alloy with a Ge concentration of 50%. This was conducted in consideration of the result by Ruiz et al. where 50% of Ge concentration is optimal for bulk devices [25]. Then, the active layer of Si$_{1-x}$Ge$_x$ is graded based on its mole fraction concentration. The alloy is varied with Ge concentrations from 86% to 90% because it is the most optimal concentration for the Si$_{1-x}$Ge$_x$ alloy [6]. For the optical parameter, Si$_{1-x}$Ge$_x$ with Ge concentration of 50% uses the absorption coefficient of Si$_{1-x}$Ge$_x$ with mole fraction ($x$) of 0.50, while Si$_{1-x}$Ge$_x$ with Ge concentration of 86%-90% uses absorption coefficient of Si$_{1-x}$Ge$_x$ with $x=1.00$ [26]. The electrical parameters of the Si$_{1-x}$Ge$_x$ layer that were used in this step are presented in Table 1, and a few of them were calculated using the following equations:

Permittivity($x$) [27]:

$$11.7 + 4.5x$$  

(1)

Bandgap energy ($E_g$)($x$) [28]:

$$
1.12 - 0.41x + 0.008 x^2 \text{ eV for } x < 0.85
$$

$$
1.86 - 1.2x \text{ eV for } x > 0.85
$$  

(2) (3)

Effective conduction/valence band concentration ($N_C/N_V$) [28]:

$$
\sim 2.8 \times 10^{19} \text{ cm}^{-3} \quad \text{for } x < 0.85
$$

$$
\sim 1.0 \times 10^{19} \text{ cm}^{-3} \quad \text{for } x > 0.85
$$  

(4) (5)

Electron affinity ($\phi$)($x$) [29]:

$$
4.05 - 0.05x \text{ eV}
$$  

(6)

Electron mobility ($\mu_n$)($x$) [30]:

$$
1500(1-x) + 3900x \text{ cm}^2/\text{Vs}^{-1}
$$  

(7)

Hole mobility ($\mu_p$)($x$) [30]:

$$
450(1-x) + 1900x \text{ cm}^2/\text{Vs}^{-1}
$$  

(8)

### Table 1. Electrical parameters of Si$_{1-x}$Ge$_x$ layer

<table>
<thead>
<tr>
<th>$x$</th>
<th>Permittivity</th>
<th>$E_g$ (eV)</th>
<th>Affinity (eV)</th>
<th>$N_C$ (cm$^{-3}$)</th>
<th>$N_V$ (cm$^{-3}$)</th>
<th>$\mu_n$ (cm$^2$/V-s)</th>
<th>$\mu_p$ (cm$^2$/V-s)</th>
</tr>
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<tbody>
<tr>
<td>0.50</td>
<td>13.950</td>
<td>0.917</td>
<td>4.0250</td>
<td>2.8x10$^{19}$</td>
<td>2.8x10$^{19}$</td>
<td>2700</td>
<td>1175</td>
</tr>
<tr>
<td>0.86</td>
<td>15.570</td>
<td>0.828</td>
<td>4.0070</td>
<td>1.0x10$^{20}$</td>
<td>1.0x10$^{20}$</td>
<td>3564</td>
<td>1697</td>
</tr>
<tr>
<td>0.87</td>
<td>15.615</td>
<td>0.816</td>
<td>4.0065</td>
<td>1.0x10$^{20}$</td>
<td>1.0x10$^{20}$</td>
<td>3588</td>
<td>1711.5</td>
</tr>
<tr>
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<td>15.660</td>
<td>0.804</td>
<td>4.0060</td>
<td>1.0x10$^{20}$</td>
<td>1.0x10$^{20}$</td>
<td>3612</td>
<td>1726</td>
</tr>
<tr>
<td>0.89</td>
<td>15.705</td>
<td>0.792</td>
<td>4.0055</td>
<td>1.0x10$^{20}$</td>
<td>1.0x10$^{20}$</td>
<td>3636</td>
<td>1740.5</td>
</tr>
<tr>
<td>0.90</td>
<td>15.750</td>
<td>0.780</td>
<td>4.0050</td>
<td>1.0x10$^{20}$</td>
<td>1.0x10$^{20}$</td>
<td>3660</td>
<td>1755</td>
</tr>
</tbody>
</table>

Optimization of triple-junction hydrogenated silicon solar cell nc-Si:H/a-Si:H/... (Nji Raden Poespawati)
Second, replacing the a-SiC layer on the p-layers of the middle and bottom junctions with a-Si. This replacement is based on the lattice constants of the materials. The a-SiC layer has a lattice constant of 3.073 Å, whereas a-Si has a lattice constant of 5.431 Å. Since a-Si has a lattice constant closer to its neighbor materials, the replacement of the a-SiC layer with a-Si reduces misfit dislocation and increases the overall efficiency of the solar cells. After all of the a-SiC layer is replaced with a-Si, the simulation is again performed with varying Si1-xGe x layers with Ge concentrations between 86% and 90%.

Finally, the Si1-xGe x active layer at the bottom of the cell is graded with the p-i layer grading on top (thickness 10 nm) and the i-n layer grading at the bottom (thickness varying from 10 nm to 360 nm). The final structure can be seen in Figure 1(c). The choice of thickness is referring to experiments conducted by Swaaij et al. [19]. To optimize the solar cell efficiency, the grading width of the p-i interface should be as small as possible, while the i-n interface should be as large as possible. The electrical parameters of the solar cell structure can be seen in Table 2.

### Table 2. Electrical parameters of the triple-junction solar cell when grading Si1-xGe x bottom absorber layer

<table>
<thead>
<tr>
<th>Layer parameters</th>
<th>Solar cell layers</th>
<th>p</th>
<th>i</th>
<th>n</th>
<th>p</th>
<th>i</th>
<th>n</th>
<th>p-i grading</th>
<th>i</th>
<th>i-n grading</th>
<th>n</th>
</tr>
</thead>
<tbody>
<tr>
<td>L (nm)</td>
<td>nc-Si:H</td>
<td>10</td>
<td>2100</td>
<td>25</td>
<td>10</td>
<td>90</td>
<td>25</td>
<td>10</td>
<td>10</td>
<td>250</td>
<td>w</td>
</tr>
<tr>
<td>Permittivity</td>
<td>nc-Si:H</td>
<td>11.9</td>
<td>11.9</td>
<td>11.9</td>
<td>11.9</td>
<td>11.9</td>
<td>11.9</td>
<td>15.57</td>
<td>15.57</td>
<td>15.75</td>
<td>14</td>
</tr>
<tr>
<td>E0 (eV)</td>
<td>nc-Si:H</td>
<td>2</td>
<td>1.95</td>
<td>1.95</td>
<td>1.82</td>
<td>1.82</td>
<td>1.82</td>
<td>0.828</td>
<td>0.828</td>
<td>0.78</td>
<td>1.4</td>
</tr>
<tr>
<td>Affinity (eV)</td>
<td>nc-Si:H</td>
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<td>4</td>
<td>4</td>
<td>3.8</td>
<td>3.8</td>
<td>3.8</td>
<td>4.007</td>
<td>4.007</td>
<td>4.005</td>
<td>4.01</td>
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<td>2.5x10²⁰</td>
<td>2.5x10²⁰</td>
<td>2.5x10²⁰</td>
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<td>1x10²⁰</td>
</tr>
<tr>
<td>Nc/cm²</td>
<td>a-Si:H</td>
<td>2.5x10²⁰</td>
<td>2.5x10²⁰</td>
<td>2.5x10²⁰</td>
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<td>1x10¹⁸</td>
<td>1x10¹⁸</td>
<td>1x10²⁰</td>
</tr>
</tbody>
</table>

### 3. RESULTS AND DISCUSSION

In the first stage, the result of a triple-junction solar cell simulation with the structure nc-Si:H/ a-Si:H/Si1-xGe x:H shows that the Si1-xGe x layer with the mole fraction x=0.89 has not only the best efficiency but also the best fill factor (FF). It also confirms that the optimum concentration of germanium in the Si1-xGe x alloy is between 86% and 90% [6]. The changes in efficiency related to the Ge mole fraction are shown in Figure 3.

![Figure 3. Efficiency versus Ge concentration for the first stage of optimization](image)

The simulation results of the second optimization show that 90% germanium concentration in the Si1-xGe x layer produces the solar cell’s highest efficiency. Figure 4 shows the changes in efficiency related to Ge mole fraction in a-Si configuration. The efficiency curve is also still in accordance with result from Koschier et al. [6]. The numbers show that the replacement of a-SiC with a-Si can reduce the misfit dislocation, which, in turn, can increase the FF of the solar cells as well as its efficiency. Misfit dislocation
Optimization of triple-junction hydrogenated silicon solar cell nc-Si:H/a-Si:H/... (Nji Raden Poespawati)

Reduction is seen in lattice constant difference when using a-SiC and after it is replaced with a-Si. In the middle junction, the lattice constant of a-SiC has a difference of 2.358 Å compared to both the nc-Si and a-Si layers. In the lower junction, the lattice constant of a-SiC has a difference of 2.557 Å relative to the Si_{1-x}Ge_x layer, while the a-Si lattice constant differs by only 0.199 Å (less than 4.2%) from the Si_{1-x}Ge_x layer. In the third stage, in theory, the addition of a grading layer on the active layer of Si_{1-x}Ge_x will affect the efficiency of solar cells in terms of the addition of the FF [19].

This can be proven by the curves of the solar cells’ open-circuit voltage ($V_{OC}$) and short-circuit current ($I_{SC}$) parameter values, which do not change when the grading thickness is varied in the Si_{1-x}Ge_x layer, see Figures 5(a)-(b). The final result for the thickness used for the i-n grading layer is 230 nm, since the highest efficiency is produced at this thickness despite the FF generated is equal to the thickness of 200 nm to 240 nm, see Figures 5(c)-(d).
Thus, the germanium mole fraction $x$ obtained for the optimum composition of the $p$-$i$ upper layer and the $i$-$n$ lower layer is 0.86 with a thickness of 10 nm and 0.90 with a thickness of 230 nm, respectively. The magnitude of the $I_{SC}$ produced by the triple-junction solar cell nc-Si:H/a-Si:H/Si$_{1-x}$Ge$_x$:H is 20.49 mA, the $V_{OC}$ is 1.13 V, and the FF is 0.83, allowing the solar cell efficiency to reach 19.08%. The final results show that there is a significant possibility of increasing the efficiency of a triple-junction solar cell with the structure nc-Si:H/a-Si:H/Si$_{1-x}$Ge$_x$:H by modifying it into a step graded Si$_{1-x}$Ge$_x$ layer. The improvement of the solar cell performance for each stage is summarized in Table 3.

<table>
<thead>
<tr>
<th>Stage</th>
<th>$V_{OC}$ (V)</th>
<th>$I_{SC}$ (mA)</th>
<th>FF</th>
<th>Efficiency (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1.13</td>
<td>20.49</td>
<td>0.64</td>
<td>14.82</td>
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<tr>
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<td>0.82</td>
<td>19.03</td>
</tr>
<tr>
<td>3</td>
<td>1.13</td>
<td>20.49</td>
<td>0.83</td>
<td>19.08</td>
</tr>
</tbody>
</table>

To give an understanding of the junction, the energy band diagram of the optimized device is presented in Figure 6. The top and bottom black lines are the valence and conduction band, respectively. The red line is the quasi-Fermi level for the holes, and the blue line is the quasi-Fermi level for the electrons. The blue lines indicated that the movement of electrons from the upper to the lower cells does not show any resistance. Usually, the resistance will occur in the junction caused by the barrier between the junctions. The lack of resistance can be caused by the thin $n$-$p$ interface layers and the large doping difference at the $n$-$p$ interface of junctions make inter-junction barriers function as a tunnel junction, which resulted in the electron traversed via this tunnel.

From a graph of recombination-generation (R-G), it can be seen there is a high rate of recombination at the interface of each cell, see Figure 7. This is one of the main problems in multijunction solar cells. At the interface of the upper and middle cells, the recombination surpasses the generations, so it can be regarded as a loss factor. Recombination also occurs in the middle and lower cell interface, but it is not surpassing the generation. The rising levels of recombination at the bottom of the cell area (below 0.3 μm) may be caused by the unevaluated $n$-type a-SiGe:H characteristics. However, this also shows that the addition of step-grading above the $n$-type a-SiGe:H layer can minimize the lattice mismatch. Despite significant increases in overall performance, the R-G graph shows a prospect of future research to suppress the recombination level on this structure.
4. CONCLUSION

The design and optimization of a triple-junction solar cell with the structure nc-Si:H/a-Si:H/Si$_{1-x}$Ge$_x$:H can increase efficiency as compared to the original design of the solar cell. In the first stage, the replacement of a-SiGe:H with Si$_{1-x}$Ge gives the optimum mole fraction of Ge. Using the Ge mole fraction $x=0.89$, the solar cell achieves its best performance with an efficiency of 14.82%. In the second stage, the replacement of a-SiC with a-Si successfully increases solar cell performance with an efficiency of 14.03%. Furthermore, it was found the optimum Ge concentration using the second stage structure is 90%. In the third stage, it was found that the optimum germanium mole fraction composition of the $p$-$i$ upper layer and $i$-$n$ lower layer at the step graded Si$_{1-x}$Ge$_x$ layer is 0.86, and 0.90, respectively, and the thicknesses are 10 nm and 230 nm, respectively. The optimized structure produces a solar cell with $I_{SC}$ of 20.49 mA, $V_{OC}$ of 1.13 V, FF of 0.83, and efficiency of 19.08%.

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REFERENCES


Optimization of triple-junction hydrogenated silicon solar cell nc-Si:H/a-Si:H/... (Nji Raden Poespawati)


[29] “The general properties of Si, Ge, SiGe, SiO2 and Si3N4,” Virginia Semiconductor, 2002.